

Minds on Math: Geometric Distributions

Consider the following situations:

i) The probability of recovering after a particular type of operation is 0.5. If 3 patients undergo this operation, what is the probability that 2 of them recover?

ii) The probability of recovering after a particular type of operation is 0.5. What is the probability, for patients undergoing this operation, that 2 of them recover?

Problem:
Contrast the situations. Tell as much as you can with reference to what you currently know about probability distributions.

Take Action: Geometric Distributions

Solve each of the situations provided on the previous slide.

i) The probability of recovering after a particular type of operation is 0.5. If 3 patients undergo this operation, what is the probability that 2 of them recover?

Solution:

As this situation can be modelled by a binomial distribution,

$$P(X = r) = \binom{n}{r} p^r q^{n-r}$$

$$P(X = 2) = \binom{3}{2} 0.5^2 0.5^1$$

$$= 3(0.5)^3$$

$$= 0.375$$

What if?

ii) The probability of recovering after a particular type of operation is 0.5. What is the probability, for patients undergoing this operation, that 2 of them recover?

Solution:

- Recall that in this situation, the number of recoveries has not been specified. Therefore, we assume a number of trials.
- The random variable, X , is defined as the number of trials before experiencing a success--all called the .
- The trials must result in failures, each having a probability of q of occurring and then one success. Because of this, need to be considered.
- The formula that defines this probability distribution--the **Geometric Distribution**--is as follows:

$$P(X = r) = q^r p$$

where...
- The expectation or expected value for this distribution is given by $E(X) = \frac{q}{p}$

Before solving, let's determine the geometric distribution for the random variable, X . As the number of trials is infinite, we'll complete the model for failures of 0, 1, and 2.

r failures before recovery	$P(X = r) = q^r p$
0	•
1	•
2	•
...	•

Pull

E.g., If we must wait through cases of 0 and 1 failures, before experiencing success then $r = 1$.

$$\therefore P(X = 1) = (0.5)^1 (0.5)$$

$$= 0.25$$

Conclusion

Geometric Distributions

Date: _____

Practice

Using the geometric formulas provided, solve the following problem.

An assembly-line robot installs a DVD player into each mini-van produced on the line. For quality control, the players are tested to make sure that they are properly installed. The robot has a probability of malfunctioning of 0.2.

- a) What is the probability that a malfunction will occur on the 5th test?

- b) What is the expected number of tests before a malfunction is found?

$$E(X) = \frac{q}{p} = \frac{0.8}{0.2} = 4$$



Attachments

Geometric Distribution.xls